

**RoboJackets**

**CAT**  
THE ARTHUR M. BLANK  
FAMILY FOUNDATION

2007 TE Sessions – Mechanical  
Energy and Fluid Power  
Oct. 30, 2007

---

---

---



---

---

---

---

---

**MECH ENERGY STORAGE**

**RoboJackets**

---

---

---



---

---

---

---

---

**Energy**  
**What is energy?**

**Energy**  
**Units:**  
Foot-pounds; Newton-meters; Joules; BTU; Calories, etc

- Energy is energy regardless of sign
- Non directional

**Sign significance**

- Energy can be stored in two ways
- Potential
- Kinetic

**Sign significance**

- Energy can be expended through work
- or dissipated (friction & heat)

**RoboJackets**

---

---

---


---

---

---

---

---




## Energy



### Potential Storage

**Potential**  
Energy can be stored as a force against gravity

- Simplest way is a force at a distance (foot-pounds)
- Raising a mass against gravity



Energy stored = mass x gravity x height  
 $E = mgh$


---

---

---


---

---

---

---

---

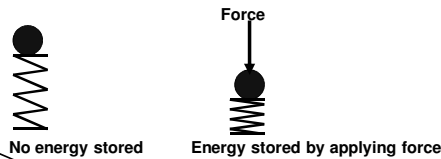


## Energy



### Potential Storage

**Potential**  
Energy can be stored as inside mechanical devices through material deflection

- Springs store energy
- Spring constant



Energy stored by applying force


---

---

---


---

---

---

---

---



## Energy

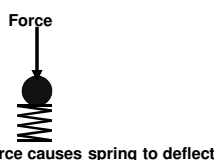
### Potential Storage

**Springs**  
Energy stored is a function of two things:



- Spring constant  $k$
- Distance of spring deflection  $x$

**Spring constant**

- $k = \text{Force/Displacement} = F/x$
- Amount of force needed to deflect spring one inch



Force causes spring to deflect


---

---

---


---

---

---


---

---



## Energy

### Potential Storage



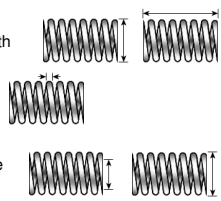
**Springs**  
Other spring definitions, terms, and specs

**Material**  
- Spring steel, music wire

**Specs**  
- Outside Diameter and length

**Specs**  
- Wire Size

**Specs**  
- Rod and Hole Size



**RoboJackets**

---

---

---


---

---

---


---

---



## Energy

### Potential Storage



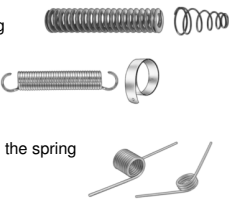
**Springs**  
Other spring definitions, terms, and specs

**Compressed Length**  
- Minimum length of spring under force

**Compression springs**  
- Forces compress the spring

**Tension**  
- Forces extend the spring

**Torsion**  
- Torques compress the spring



**RoboJackets**

---

---

---


---

---

---


---

---



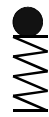
## Energy

### Potential Storage




**Potential**  
Energy can be stored as inside mechanical devices through spring deflection

- Energy stored =  $\frac{1}{2} k x^2$



No energy stored



Energy stored by applying force

**RoboJackets**

---

---

---


---

---

---


---

---



## Energy

### Potential Storage




Example

- Energy stored =  $\frac{1}{2} k x^2$
- $k = 20 \text{ lbf/in}$
- Desired energy = 100 ft-lbf
- How far must spring be compressed?

- $100 \text{ ft-lbf} = \frac{1}{2} 20 \text{ lbf/in } x^2$
- $x = 3.16 \text{ inches}$

Energy storage is quadratic, not linear



---

---

---


---

---

---


---

---




## Energy

### Potential Storage



Other Potential Storage Mechanisms

- Compressed gas  
Air compressors store air in large tanks  
Stored air is used in large quantities by tools
- Fuel  
Hydrocarbons (gasoline, propane, etc)  
Fuel is chemically stored energy
- Batteries  
Batteries store energy as chemical electricity  
Batteries can be recharged by adding energy



---

---

---


---

---

---


---

---



## Energy


### Kinetic Energy



What is kinetic energy?

- Kinetic energy is in motion
- All mass in motion has kinetic energy

- Falling/Moving mass  
Mass in motion has energy proportional to its mass and speed
- Rotating mass  
Spinning mass has energy proportional to its inertia and rpm



---

---

---


---

---

---


---

---



## Energy


### Kinetic Energy



- Kinetic energy is in motion
- All mass in motion has kinetic energy

- Falling/Moving mass  
Mass in motion has energy proportional to its mass and speed

- Rotating mass  
Spinning mass has energy proportional to its inertia and rpm




---

---

---


---

---

---


---

---



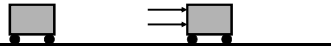
## Energy

### Kinetic Energy




Mass in motion

- Energy =  $\frac{1}{2}$  mass x velocity<sup>2</sup>
- $E = \frac{1}{2} mv^2$



- Energy increases quadratically with velocity
- Energy increases linearly with mass




---

---

---


---

---

---


---

---



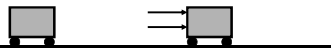
## Energy

### Kinetic Energy




Example

- 20kg mass moving at 10 m/s
- $E = \frac{1}{2} mv^2$



Energy required =  $\frac{1}{2} \times 20\text{kg} \times (10\text{m/s})^2$   
 $E = 1000 \text{ Joules (N-m)}$




---

---

---


---

---

---


---

---




## Energy

### Kinetic Energy



- Flywheels
  - Flywheels store kinetic energy by spinning
  - Examples: engine flywheel, saw blade, governor
- Rotating mass energy:
  - Energy =  $\frac{1}{2} I \omega^2$
  - I = moment of inertia
  - $\omega$  = angular velocity (rad/s)




---

---

---


---

---

---


---

---

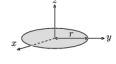



## Energy

### Kinetic Energy



- Flywheels
  - Example:
    - 5kg, 0.2m diameter, thin disc spinning at 100 rad/s
    - How much energy is it storing?
  - First calculate its moment of inertia:
    - $I_z = \frac{1}{2} m r^2$
    - $I_z = \frac{1}{2} 5\text{kg} (0.1\text{m})^2 = 0.025\text{kg}\cdot\text{m}^2$
  - Calculate kinetic energy stored:
    - $E = \frac{1}{2} I \omega^2$
    - $E = \frac{1}{2} (0.025\text{kg}\cdot\text{m})(100\text{rad/s})^2$
    - $E = 125 \text{ Joules}$


---

---

---


---

---

---


---

---

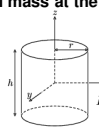


## Energy


### Kinetic Energy



- Notes on spinning masses:
  - Energy increases quadratically with angular velocity (rpm)
  - Energy increases linearly with inertia
  - Inertia increases linearly with mass
  - Inertia increases quadratically with radius
- Greater inertia effects from having all mass at the edge of flywheel



$$I_z = \frac{mr^2}{2}$$

$$I_x = I_y = \frac{1}{12} m (3r^2 + h^2)$$



---

---

---


---

---


---

---

---

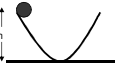


## Energy Dissipation

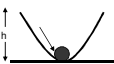


Where does energy go???

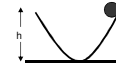
First an example on ideal energy conversion:



$PE = mgh$   
 $KE = 0$  ( $v = 0$ )



$PE = 0$  ( $h = 0$ )  
 $KE = \frac{1}{2}mv^2$



$PE = mgh$   
 $KE = 0$  ( $v = 0$ )

Ideally,  $mgh = \frac{1}{2}mv^2$  and potential is fully converted into kinetic, then back to potential, infinitely

**RoboJackets**

---

---

---


---

---


---

---

---



## Energy Dissipation



Conservation Of Energy  
FOUNDING PRINCIPLE OF THE UNIVERSE!!!  
Energy in = Energy out ALWAYS!!!

- Energy is never perfectly converted though
- Efficiency % =  $\frac{\text{mechanical energy output}}{\text{mechanical energy input}}$

Sources of loss:

- Friction
- Heat loss
- Noise

Most energy is lost through friction and heat generation

**RoboJackets**

---

---

---


---

---


---

---

---




## Energy Dissipation



Efficiency Example

A mass slides down a slope, reaching a final velocity  
 $m = 10 \text{ kg}$ ,  $h = 2 \text{ m}$ ,  $v_f = 5 \text{ m/s}$



$PE = mgh$   
 $KE = \frac{1}{2}mv^2$

Initial potential energy:  
 $PE_0 = mgh = (10\text{kg})(9.81\text{m/s}^2)(2\text{m}) = 196.2 \text{ J}$

Initial kinetic energy:  
 $KE_0 = \frac{1}{2}mv^2 = (1/2)(10\text{kg})(0\text{m/s}) = 0\text{J}$

Final potential energy:  
 $PE_f = mgh = (10\text{kg})(9.81\text{m/s}^2)(0\text{m}) = 0 \text{ J}$

Final kinetic energy:  
 $KE_f = \frac{1}{2}mv^2 = (1/2)(10\text{kg})(5\text{m/s})^2 = 125 \text{ J}$

Efficiency = Final total energy / Initial total energy:  
 $\text{eff}\% = (125 \text{ J}) / (196.2 \text{ J}) = 63.7\%$

**RoboJackets**

---

---

---


---

---

---


---

---



## Energy

### Storage and Conversion


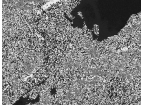



**DEMO**

Energy is stored in a spring, then released  
Converting its potential energy to kinetic energy of a smaller body

Other energy converters:

- Trebuchet, catapult (potential → kinetic)
- Generator (kinetic → electric potential)
- Engine (chemical potential → kinetic)
- Motor (electric potential → kinetic)
- Air compressor (kinetic → potential)



**RoboJackets**

---

---

---


---

---

---


---

---



## Activity # 1

### 30 minutes



**CATAPULT!!!**

Store some potential energy and convert it to kinetic energy!

Ammo: Vex gear (36 tooth)

Build a catapult using gravity to fling a Vex gear

Distance will be judged from where the gear first hits ground

Be quick though! You have 25 MINUTES starting NOW

**RoboJackets**

---

---

---


---

---


---

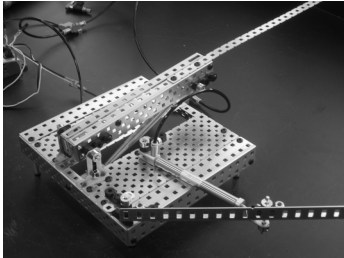
---

---



## Demo of example





**RoboJackets**

---

---

---

---



---

---


---

---



## FLUID POWER




---

---

---


---

---


---

---


---



## What is Fluid Power?



- Pressurized fluid does the work
- Hydraulics
  - Oil
  - Water
  - Other fluids
- Pneumatics
  - Air
  - Nitrogen
  - Hot gases
  - Other gases




---

---

---


---

---


---

---


---



## When to use fluid power



- Electric
  - High speed but low torque (force) → requires gears
  - Control is often more precise and rapid and less expensive
- Hydraulic and pneumatic
  - Speed/torque combo is well suited to many motion applications
  - Well suited to high forces
  - Can be delivered “around the corner”
  - Control is usually by throttling, hence wastes energy
- Center for Compact Efficient Fluid Power
  - A brazen commercial




---

---

---


---

---


---




---



---




### Hydraulics is Especially critical to the Mobile Equipment Industry





Have O-Series Tractor-Type Tractor

---

---

---


---

---


---



---



---




### Mobile equipment (construction)





---

---

---


---

---


---

---


---




### Pneumatics compared to hydraulics



- No problems of a spills
- Compressibility stores energy
  - Available for your use
  - Dangerous if excessive volumes or pressures
- Difficult to control precisely
- Fluid is readily available
  - Should be filtered, dry
- Usually lower forces



**Safety Must Always Be Considered!**



---

---

---

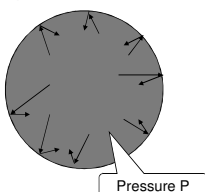
---

---

---

---

---



### Pressure of an "ideal" Gas

- Pressure of a gas is due to the force of gas molecules bouncing off the walls.
- Pressure increases when molecules are moving faster, heavier, or if there are more molecules.
- Molecules move faster when they are hot.
- $mR$  depends on molecule.

$P \times V = mR \times T$

**RoboJackets**

---

---

---


---

---

---

---

---



### Getting Work out of Air

- Work is force acting over a distance of motion, e.g. Newton x meters
- Put air in a container under pressure
- Allow part of the container to expand
- The expanding part does work

**RoboJackets**

---

---

---


---

---

---

---

---



### How much energy is in your tank?

- Tank Volume = 150 ml or 9.154 in<sup>3</sup>
- Pressure = 413,700 Pa or 60 psi
- Atmospheric pressure = 101,325 Pa or 14.7 psi
- Answer:
  - Assume constant temperature:  
 $PV = mRT = \text{constant}$
  - Work =  $PV \ln(P/P_{\text{atm}})$   
 $= 0.15 \times 413,700 \times \ln(4.083) = 87.3 \text{ kJ}$

**RoboJackets**

---

---

---


---

---


---

---

---



### Alternative Work Possibilities



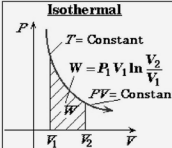
$W = \int_{V_1}^{V_2} P(V) dV$

**Isothermal**

$T = \text{Constant}$

$W = P_1 V_1 \ln \frac{V_2}{V_1}$

$PF = \text{Constant}$



Blowup of the PV diagram for Isothermals

$P = \frac{nRT}{V}$

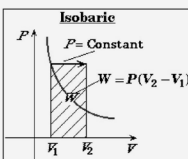
$W = \int_{V_1}^{V_2} P dV = \int_{V_1}^{V_2} \frac{nRT}{V} dV$

$= nRT \int_{V_1}^{V_2} \frac{dV}{V} = nRT \ln \frac{V_2}{V_1}$

**Isobaric**

$P = \text{Constant}$

$W = P(V_2 - V_1)$



$P = \text{Constant}$

$W = \int_{V_1}^{V_2} P dV = P \int_{V_1}^{V_2} dV$

$= P \Delta V$

**RoboJackets**

---

---

---


---

---


---

---

---



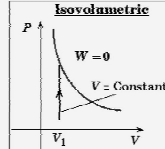
### More work possibilities



**Isochoric**

$W = 0$

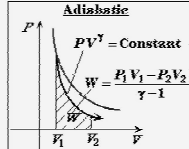
$V = \text{Constant}$



**Adiabatic**

$PV^\gamma = \text{Constant}$

$W = \frac{P_1 V_1 - P_2 V_2}{\gamma - 1}$



<http://www.calpoly.edu/~center/phys/teach/Topics/Thermodynamics/Work/Work117.PPT>

**RoboJackets**

---

---

---


---

---


---

---

---



### How much energy in your tank can you use?



- Line losses:  
Pressure drop proportional to flow
- Throttling losses:  
Pressure drop proportional to flow squared
- Cylinder friction:  
Coulomb plus viscous friction, depends on seals

**RoboJackets**

---

---

---


---

---


---

---

---



## Force available



- Pressure x Area = Force
- Area =  $\pi \times \text{Bore}^2 / 4$
- For Vex cylinder:
  - Bore = 10 mm  $\rightarrow$  Area = 78.5 mm<sup>2</sup>
  - Force = 413,700 x 78.5 x 10<sup>-6</sup> = 32.48 N
  - at 100 psi: F = 54 N

**RoboJackets**

---

---

---


---

---


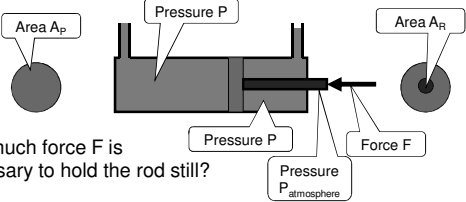
---

---

---



## The Effect of Different Areas

How much force F is necessary to hold the rod still?

**RoboJackets**

---

---

---


---

---


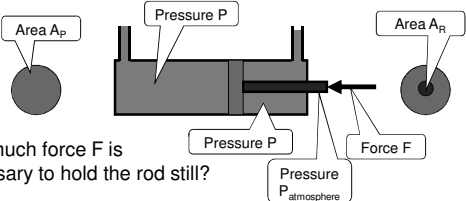
---

---

---



## The Effect of Different Areas

How much force F is necessary to hold the rod still?

Answer: Force to the right = Force to the left

$$P \times A_P = P \times (A_P - A_R) + P_{atm} \times A_R + F$$

$$F = A_R \times (P - P_{atm})$$

**RoboJackets**

---

---

---

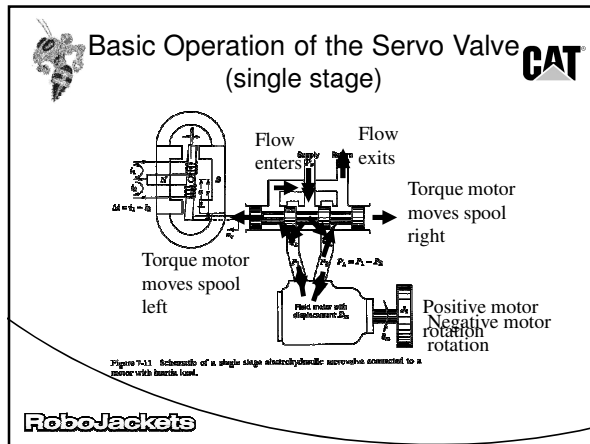
---

---

---

---

---



---

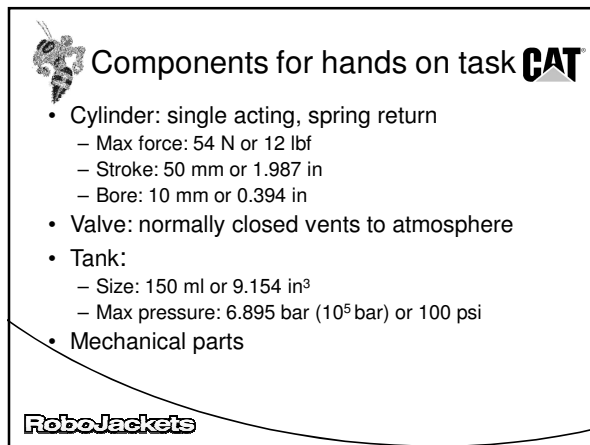
---

---

---

---

---



---

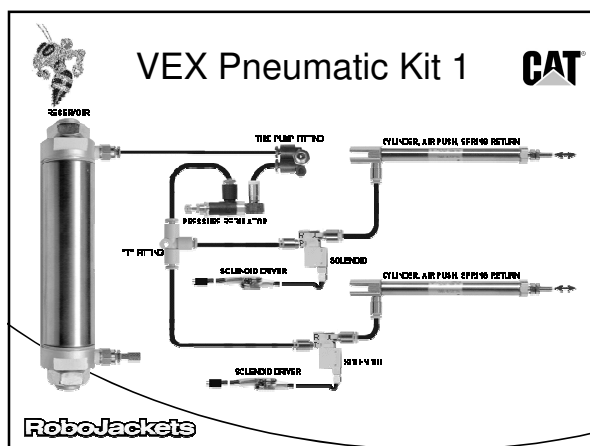
---

---

---

---

---



---

---

---

---

---

---



## Today's Challenge



- Maximum distance launch of 1 Vex gear
- Rules
  - The reservoir shall be charged at 60 psi
  - The base shall remain immobile
  - Only fluid power actuators (pistons) shall be used
  - The best out of three launches shall be considered

RoboJackets

---

---

---

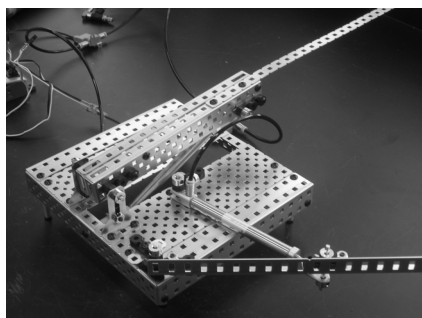
---

---

---

---

---



RoboJackets

---

---

---

---

---

---

---

---



## An example design



- Consider different configurations than the one shown?
  - two cylinders in parallel or in series
  - different linkage configurations to achieve higher speeds
  - making the lever as light as possible
  - taking advantage of flexibility to achieve higher release speeds...

RoboJackets

---

---

---


---

---

---

---

---



## Today's Challenge # 2

- Maximum distance launch of 1 Vex gear
- Rules
  - The reservoir shall be charged at 60 psi
  - The base shall remain immobile
  - Only fluid power actuators (pistons) shall be used
  - The best out of three launches shall be considered

**RoboJackets**

---

---

---

---

---

---

---

---



## Some YouTube Videos

- [http://www.youtube.com/watch?v=jkft2qaKv\\_o](http://www.youtube.com/watch?v=jkft2qaKv_o)
- <http://www.youtube.com/watch?v=0gk-yQ1H3M8>
- <http://www.youtube.com/watch?v=7l0qlO7y6Cc>
- <http://www.youtube.com/watch?v=2cluuplWRIQ>

**RoboJackets**

---

---

---


---

---

---

---

---



## Legal

These slides and more are available at  
<http://www.robojackets.org>

All media included is either in the public domain, generated by the author/s or covered by Fair Use of Copyrighted Material for Educational Purposes Title 17 Chapter 1 § 107 (which is reproduced in the next slide).

For more information contact the RoboJackets.  
 (contact info available via the web)

**RoboJackets**

---

---

---

---


---

---


---

---





Legal



Title 17 Chapter 1 § 107. Limitations on exclusive rights: Fair use

Notwithstanding the provisions of sections 106 and 106A, the fair use of a copyrighted work, including such use by reproduction in copies or phonorecords or by any other means specified by that section, for purposes such as criticism, comment, news reporting, teaching (including multiple copies for classroom use), scholarship, or research, is not an infringement of copyright. In determining whether the use made of a work in any particular case is a fair use the factors to be considered shall include—

- (1) the purpose and character of the use, including whether such use is of a commercial nature or is for nonprofit educational purposes;
- (2) the nature of the copyrighted work;
- (3) the amount and substantiality of the portion used in relation to the copyrighted work as a whole; and
- (4) the effect of the use upon the potential market for or value of the copyrighted work.

The fact that a work is unpublished shall not itself bar a finding of fair use if such finding is made upon consideration of all the above factors.

RoboJackets

---

---

---

---

---

---

---

---